

Forschergruppenkolloquium  
Institut für Geowissenschaften, Christian-Albrechts-Universität Kiel

# Investigation of dislocations and vacancy clusters by means of positron annihilation

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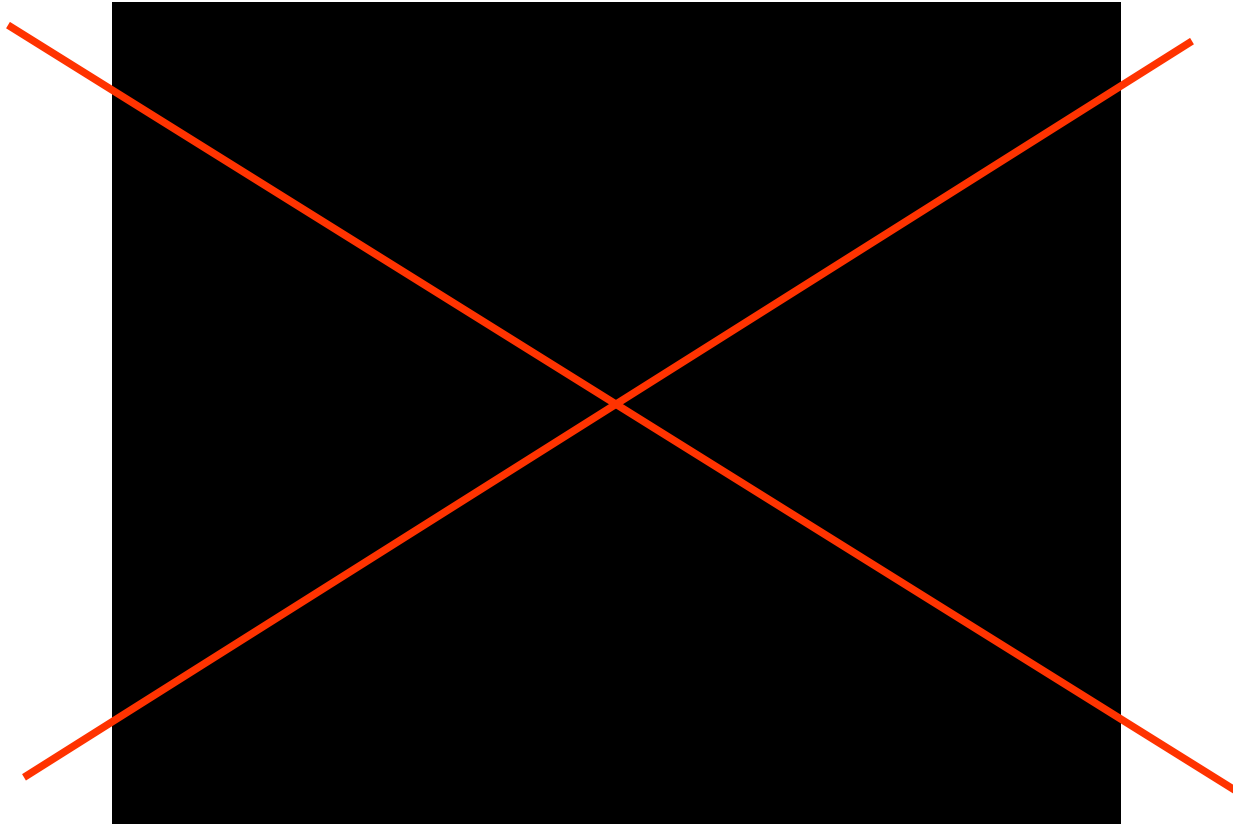
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# Overview

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- Dislocations in semiconductors – core structure
- Dislocation dynamics – plastic deformation
- Formation of point defects during plastic deformation
- What we can learn from positron annihilation about defect structures?
- Calculations of vacancy clusters
- Modell of point defect generation

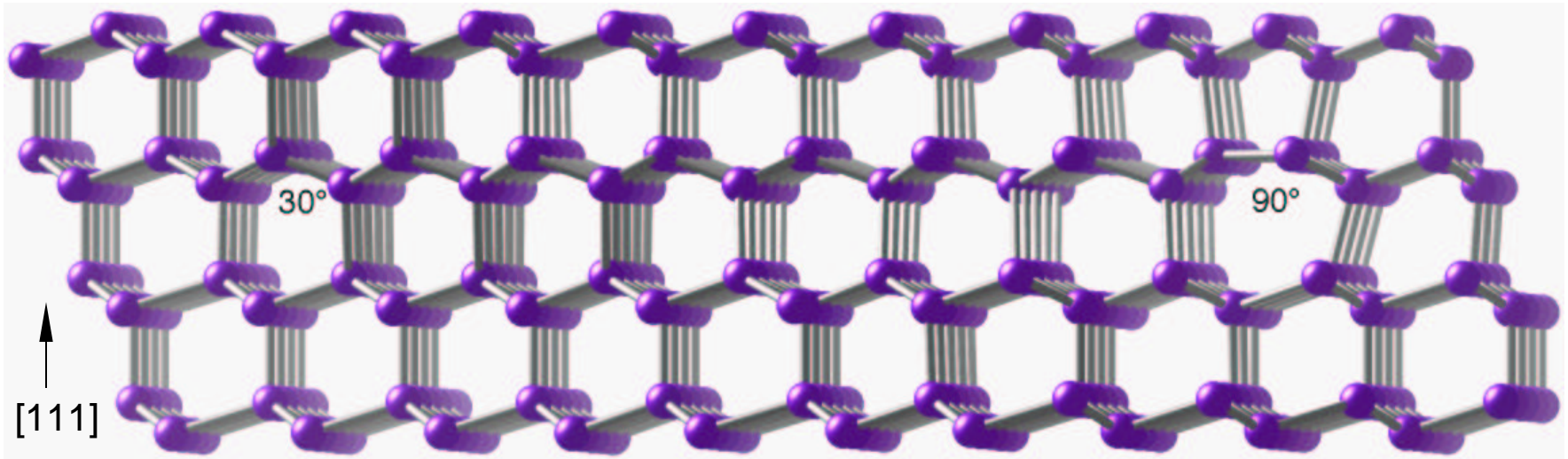
# Core structure of dislocations



60° dislocation in the diamond structure,  $\mathbf{b} = \frac{a}{2}\langle 110 \rangle$ .  
[Shockley 1953]

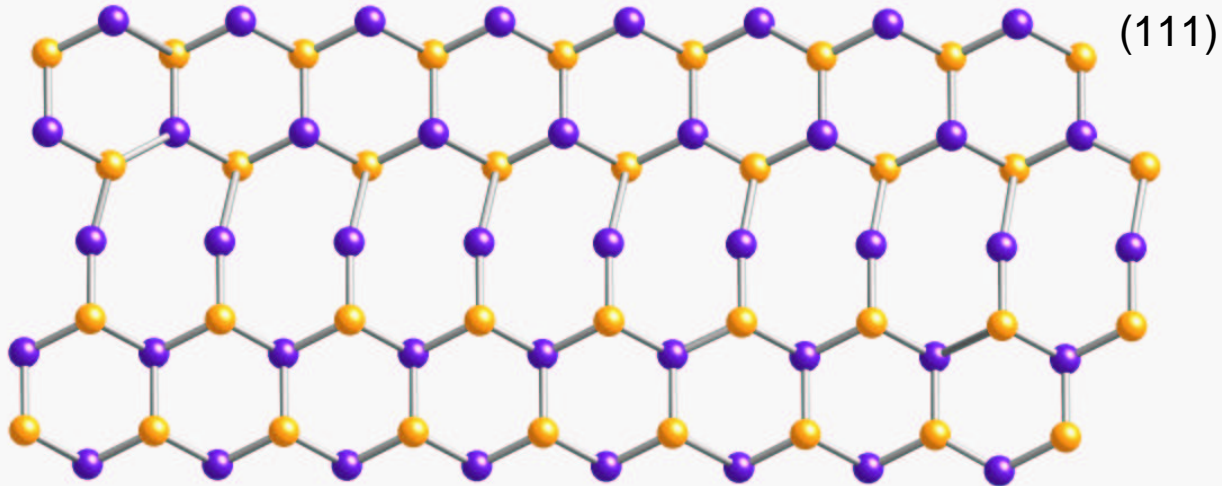
Not like this !

# Dissociation

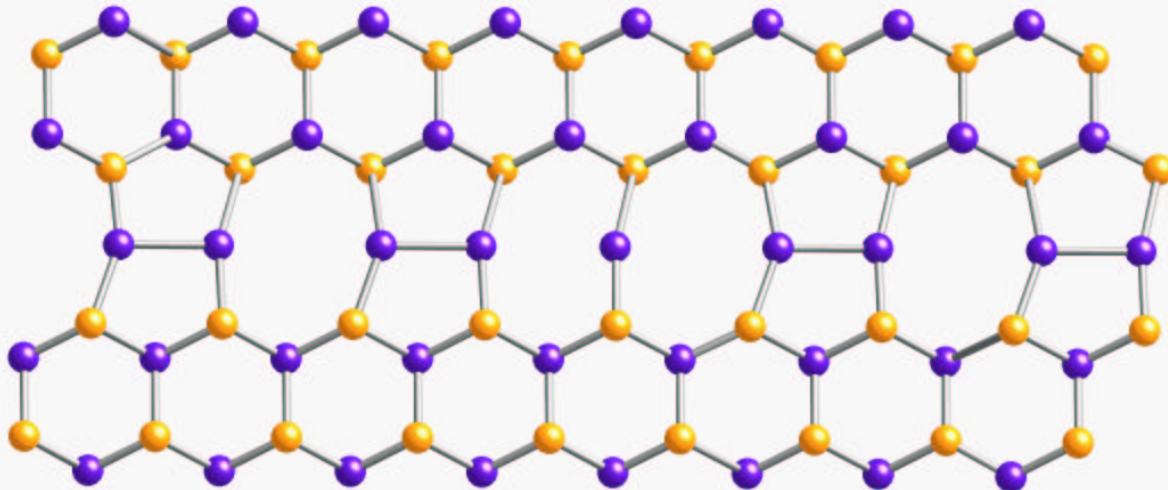


Dissociation of a perfect  $60^\circ$  dislocation in the glide set in a  $30^\circ$  and a  $90^\circ$  partial dislocation. There is an intrinsic stacking fault between the two partials. The drawing is along the  $(1\bar{1}0)$  plane.

# Reconstruction

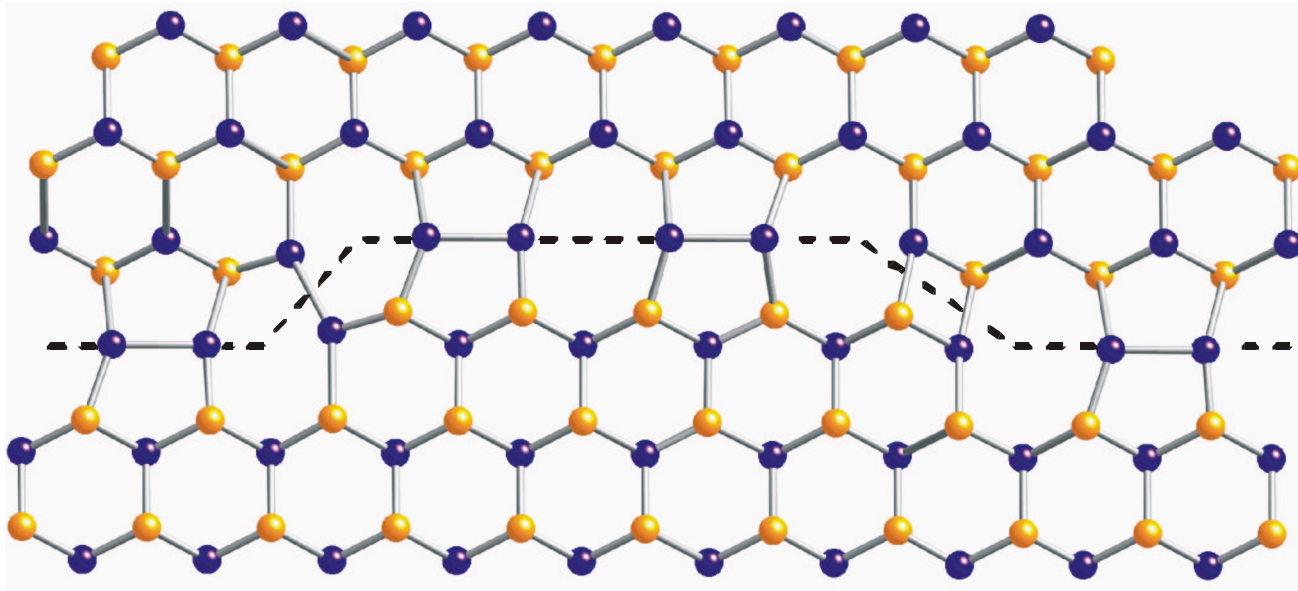


Unreconstructed  
30° partial dislocation



Reconstructed  
30° partial dislocation

# Dislocation defects



Kink pair on a  $30^\circ$  partial dislocation

# Analysis of the stress–strain curve

- *Dislocation velocity*

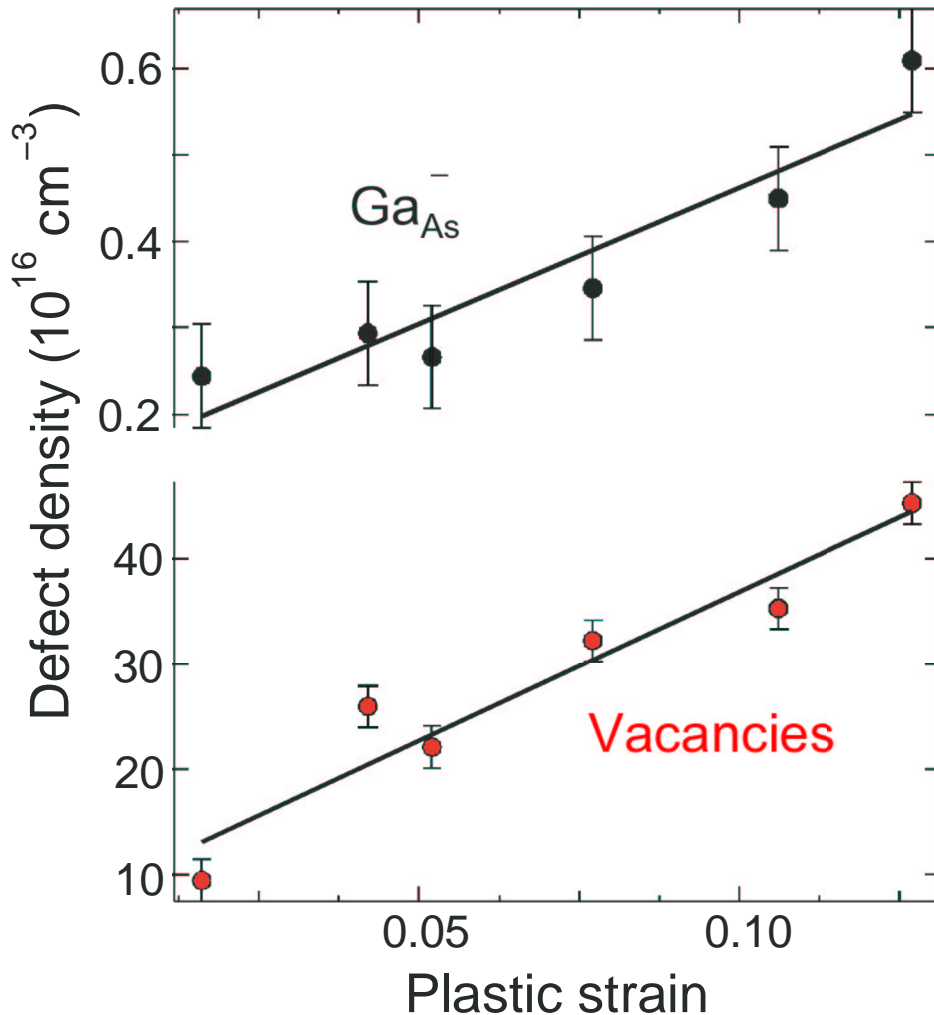
$$v = B \tau_{\text{eff}}^m \exp\left(-\frac{U}{k_B T}\right)$$

- *Lower yield stress*

$$\tau_{\text{ly}} = C \dot{\epsilon}^{1/(2+m)} \exp\left[\frac{U}{(2+m)k_B T}\right]$$

|      | $2 + m$ | $U/\text{eV}$ | $Q_d/\text{eV}$ | $Q_d/U$ |
|------|---------|---------------|-----------------|---------|
| Si   | 2.3     | 2.30          | 3.5             | 1.52    |
| InSb | 3.1     | 0.96          | 1.5             | 1.56    |
| InP  | 2.9     | 1.43          | 2.3             | 1.61    |
| GaAs | 3.6     | 1.35          | 2.0             | 1.48    |
| GaSb | 3.0     | 1.20          | 1.7             | 1.42    |

# Point defect density as a function of deformation conditions (i)



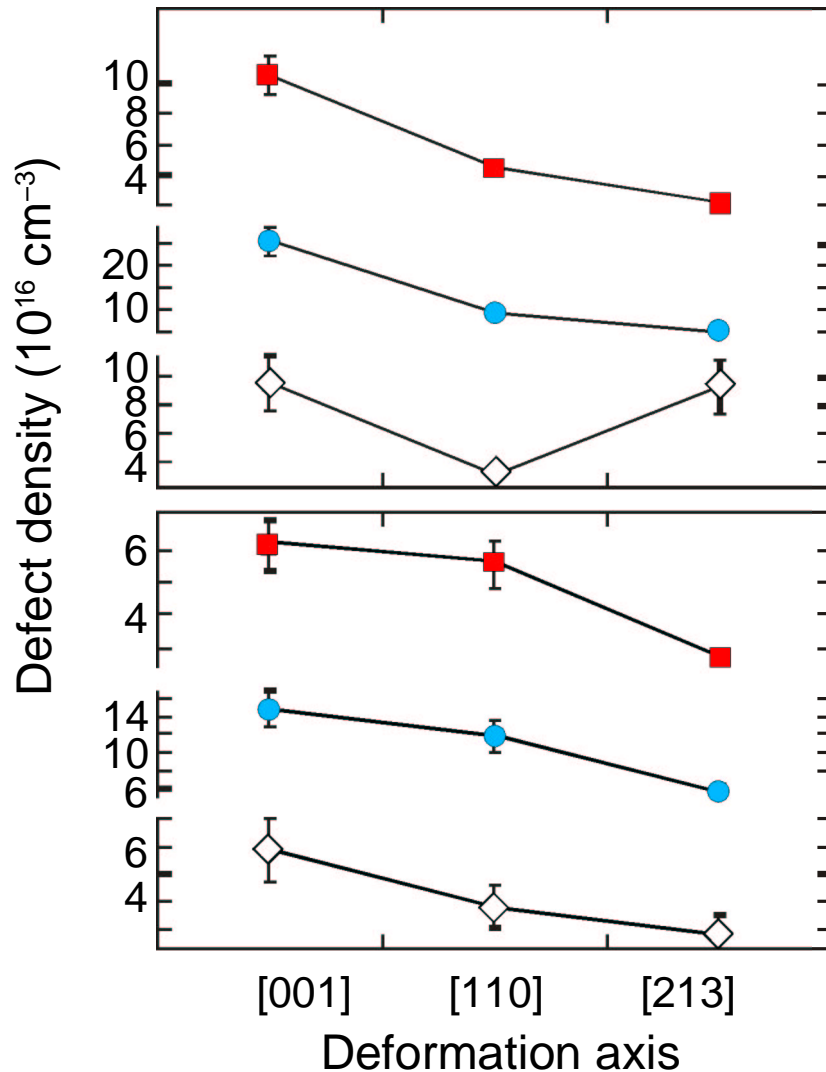
Density of vacancies and antisite defects as a function of the strain. Result of measurements by positron annihilation in plastically deformed GaAs. Uniaxial compression in [110] direction at 773 K, strain rate  $1 \times 10^{-3} \text{ s}^{-1}$ .

*Relation between excess vacancy density and strain*

$$\rho_v = \frac{l_g \zeta c_j}{l b^2 m} \varepsilon$$

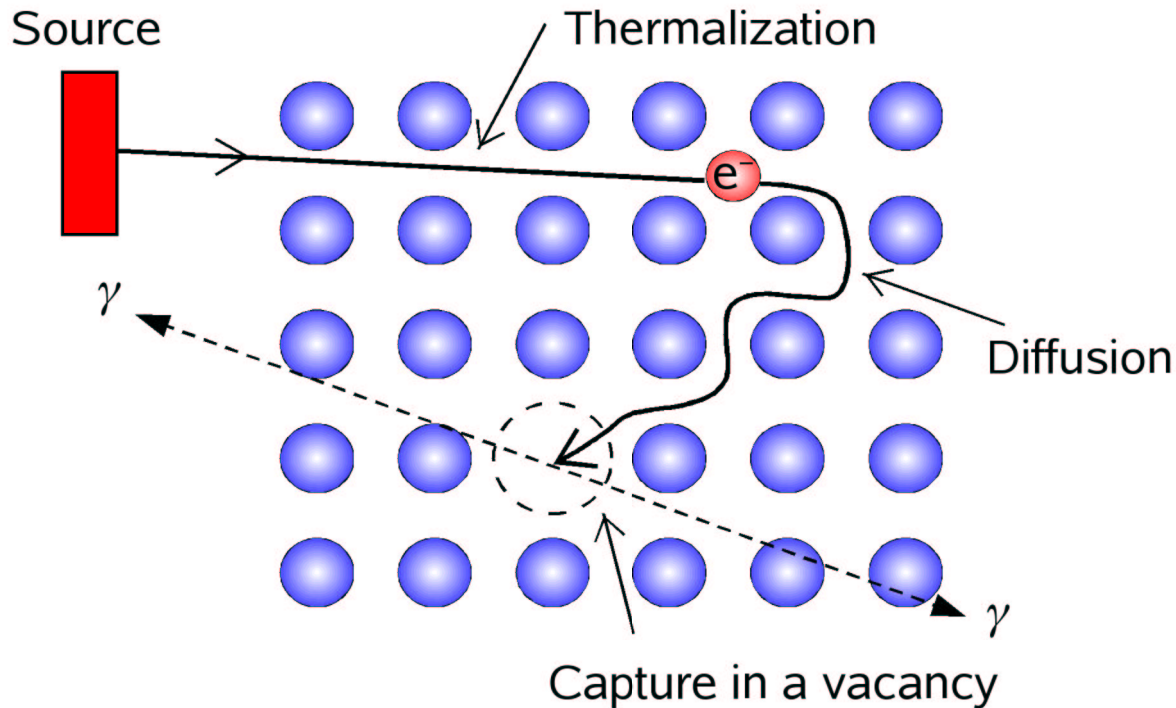


# Point defect density as a function of deformation conditions (ii)



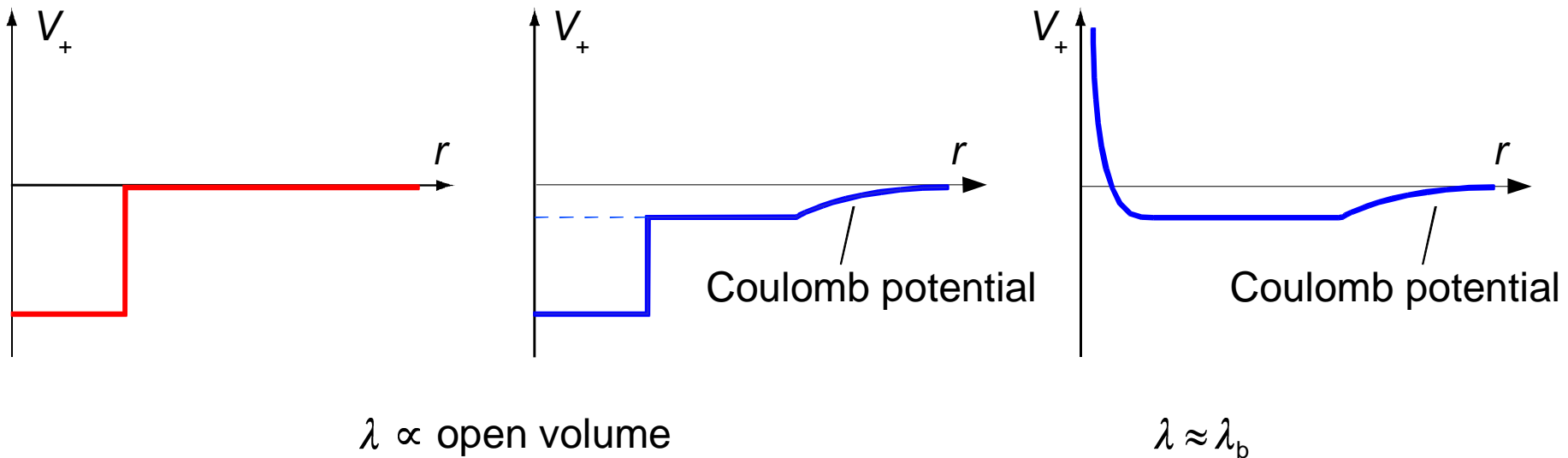
Total number of vacancies in the bulk ( $\square$ ), vacancies bound at dislocations ( $\circ$ ), as well as number of Ga<sub>As</sub> antisites ( $\diamond$ ) in plastically deformed GaAs. Deformation temperature 773 K, strain 3 %, strain rate  $7.5 \times 10^{-5} \text{ s}^{-1}$  (*above*),  $3 \times 10^{-4} \text{ s}^{-1}$  (*below*).

# Positron annihilation



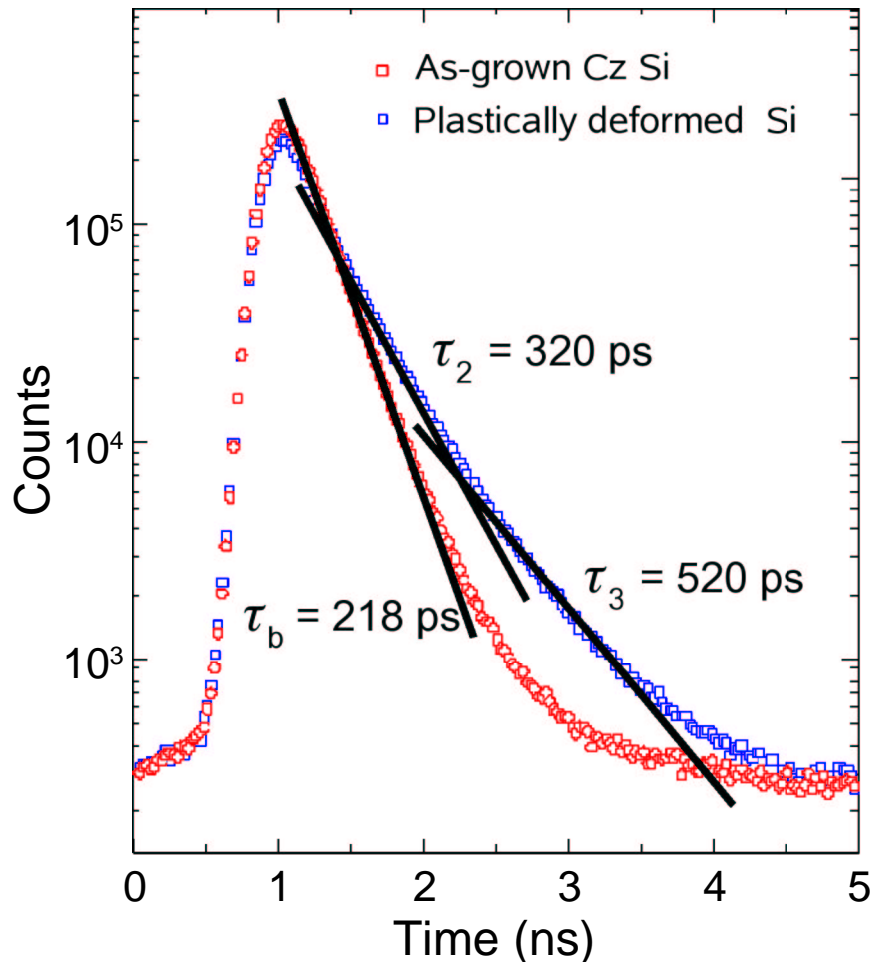
- Positrons may be captured during their diffusion in lattice defects.
- Annihilation rate (reciprocal lifetime) depends on the local electron density distribution at the annihilation site.

# Positron capture in defects



Positron potential  $V_+(r)$  of a neutral and a negatively charged vacancy. The potential of a negatively charged acceptor acting as a shallow positron trap is shown on the right.  $\lambda$  is the annihilation rate (inverse positron lifetime).

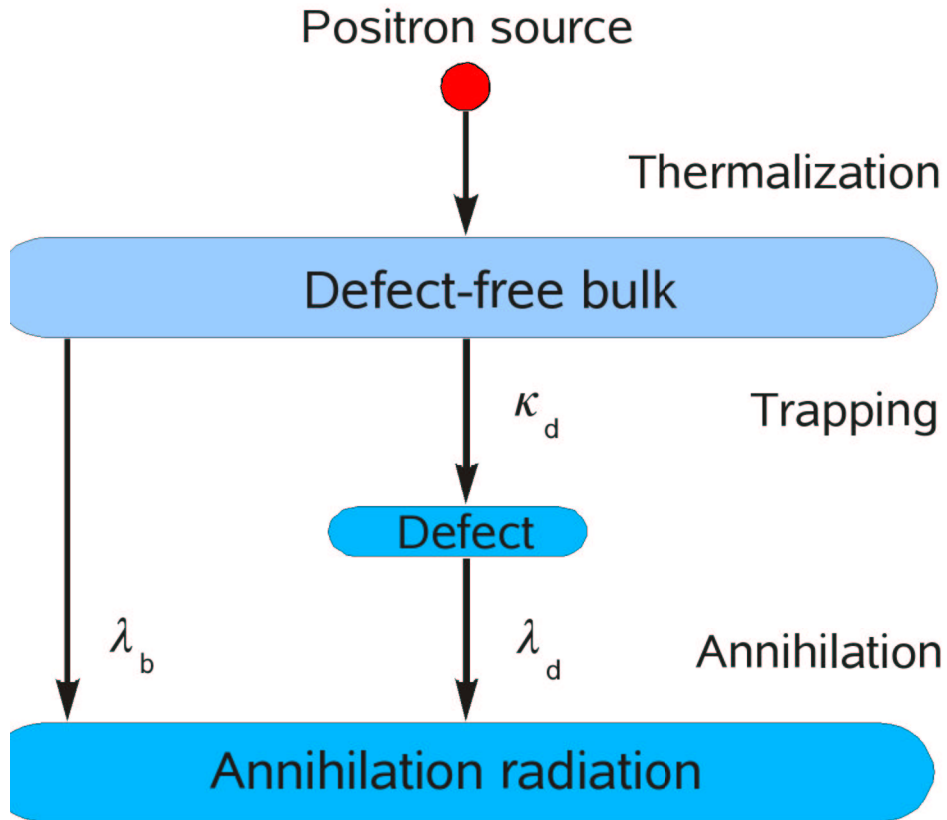
# Positron lifetime spectrum



## *Decomposition of experimental positron lifetime spectra:*

- Undeformed Czochralski Si:  
one component,  $\tau_b = 218$  ps
- Plastically deformed Si:  
(3 %, 1050 K)  
three components  
 $\tau_1 = 120$  ps (not shown),  
 $\tau_2 = 320$  ps,  $\tau_3 = 520$  ps

# Trapping model



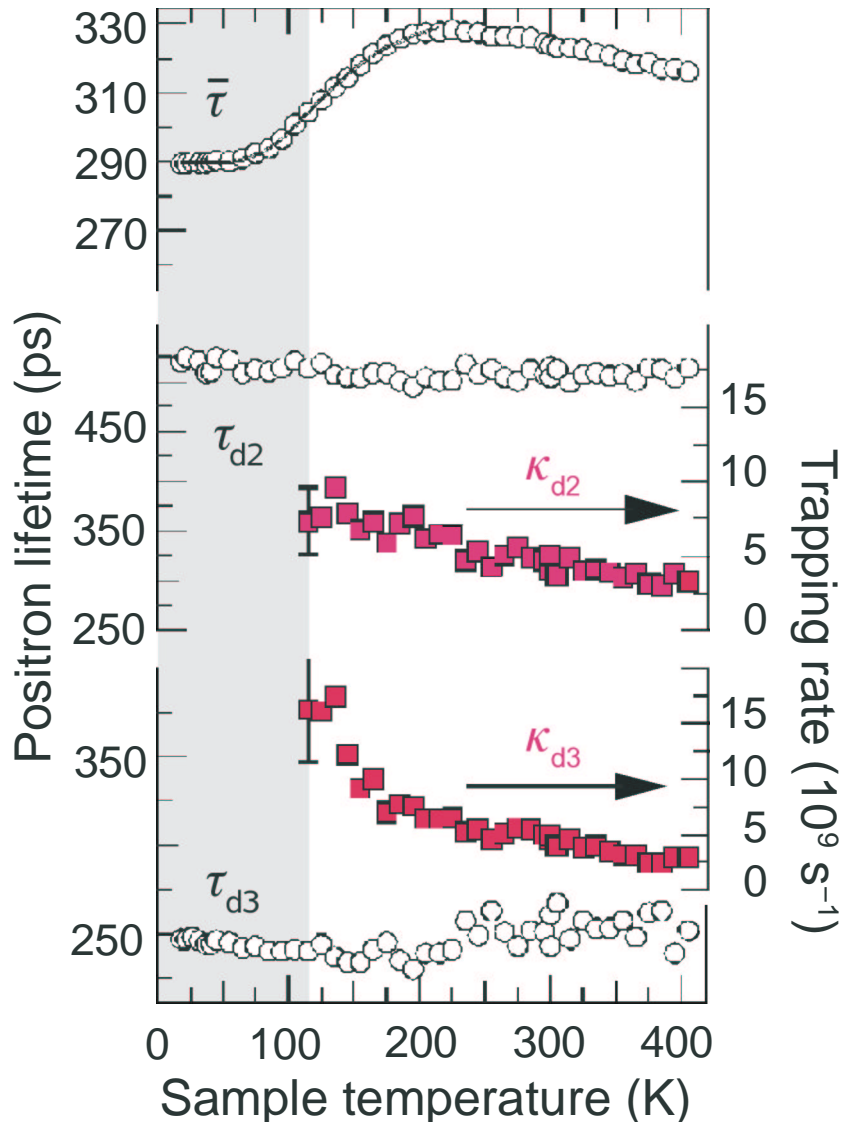
- Quantitative analysis of positron trapping by a set of rate equations
- Solution (lifetime spectrum):

$$\sum_i \frac{I_i}{\tau_i} \exp\left(-\frac{t}{\tau_i}\right)$$

$$\text{Trapping rate: } \kappa_d = \mu C_d$$

$$\text{Average positron lifetime: } \bar{\tau} = \sum_i I_i \tau_i$$

# Positron lifetimes and capture rates in deformed GaAs



## *Lifetime components:*

➤  $\tau_2 = \tau_{d3} = (260 \pm 5) \text{ ps}$

corresponds to a defect with the open volume of a monovacancy

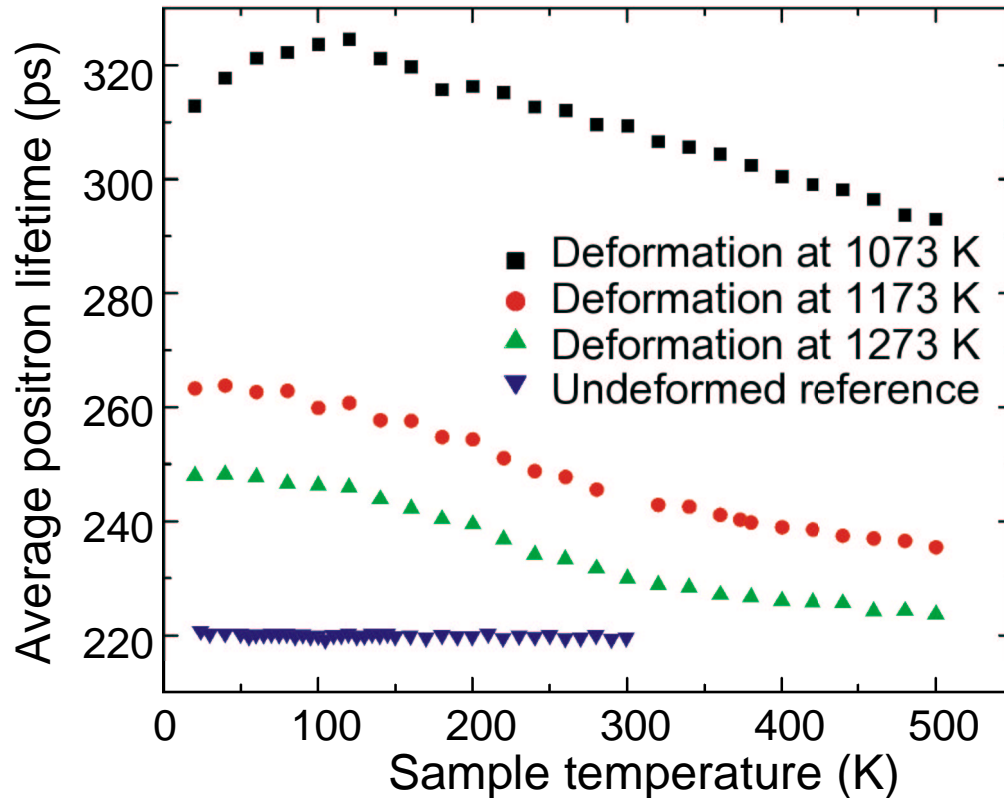
➤  $\tau_3 = \tau_{d2} = (477 \pm 20) \text{ ps}$

corresponds to a defect with a large open volume (vacancy cluster)

➤ At low sample temperatures, another positron trap without open volume becomes active (*e. g.* antisite defects).

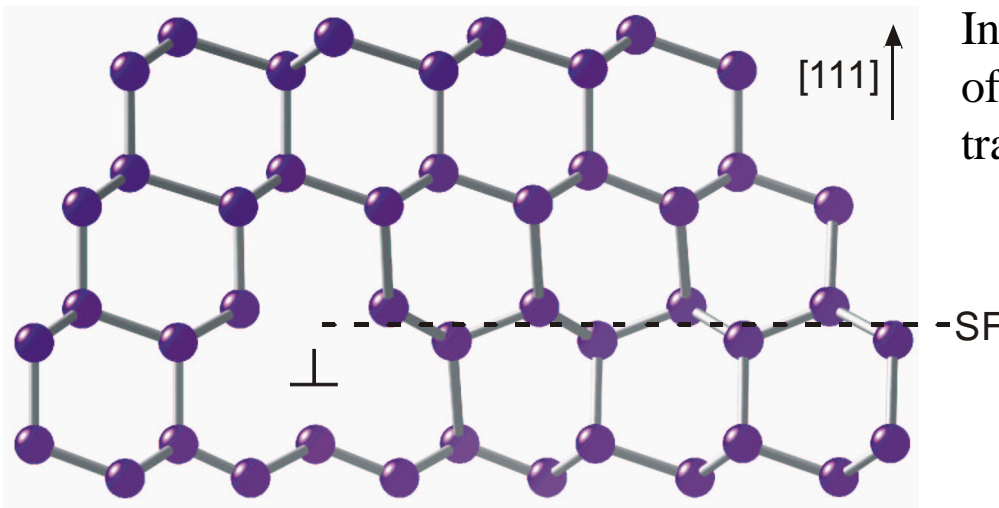
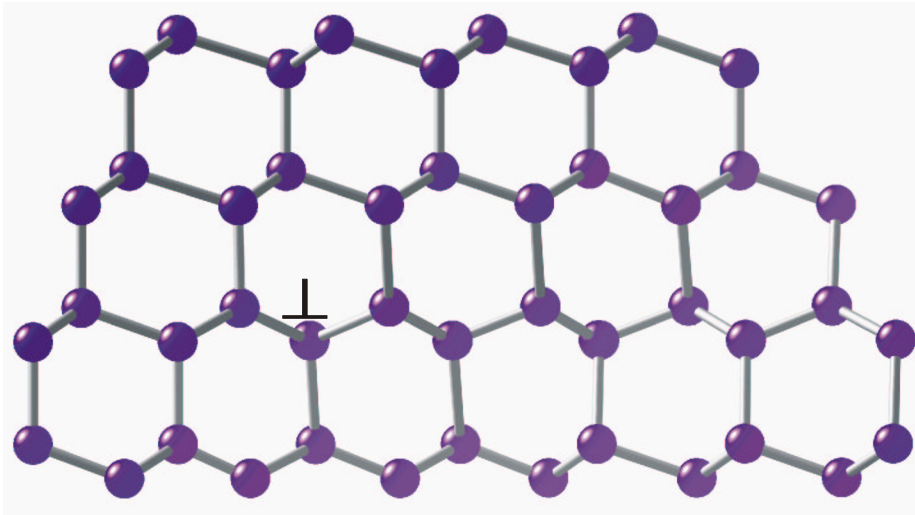
$$\tau_{d1} \approx \tau_b$$

# Plastic deformation of silicon



Average positron lifetime as a function of the sample temperature in lightly P-doped FZ Si deformed in [110] direction. 7 % deformation,  $2.1 \times 10^{-5} \text{ s}^{-1}$  strain rate.

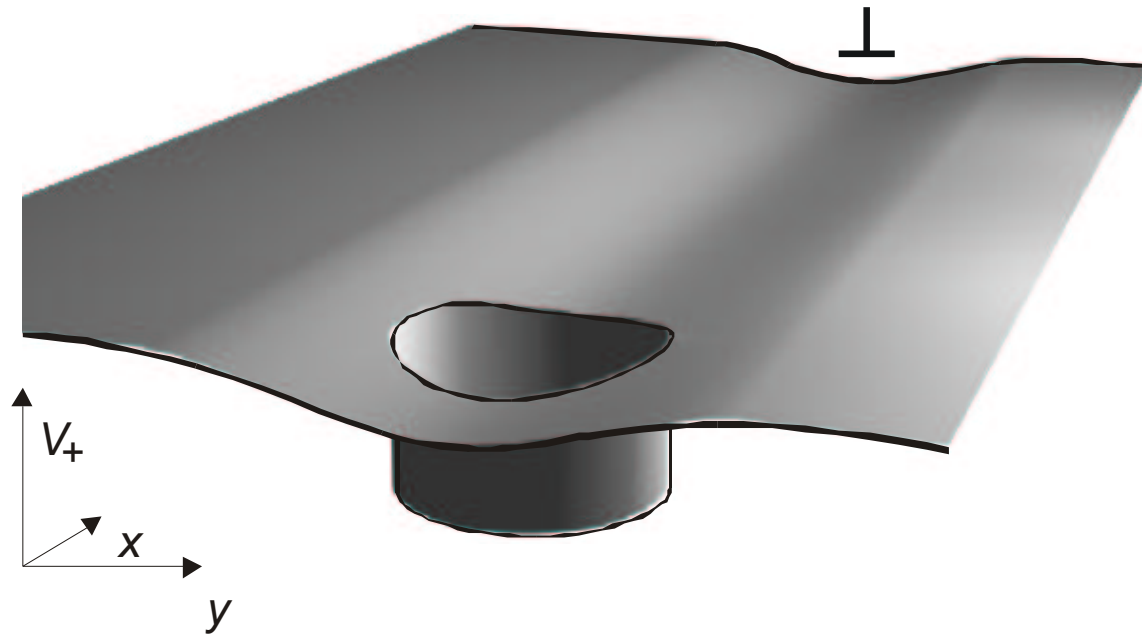
# Vacancy incorporation in dislocations



Incorporation of a vacancy in the core of a  $30^\circ$  partial dislocation as a local transition from glide to shuffle set.

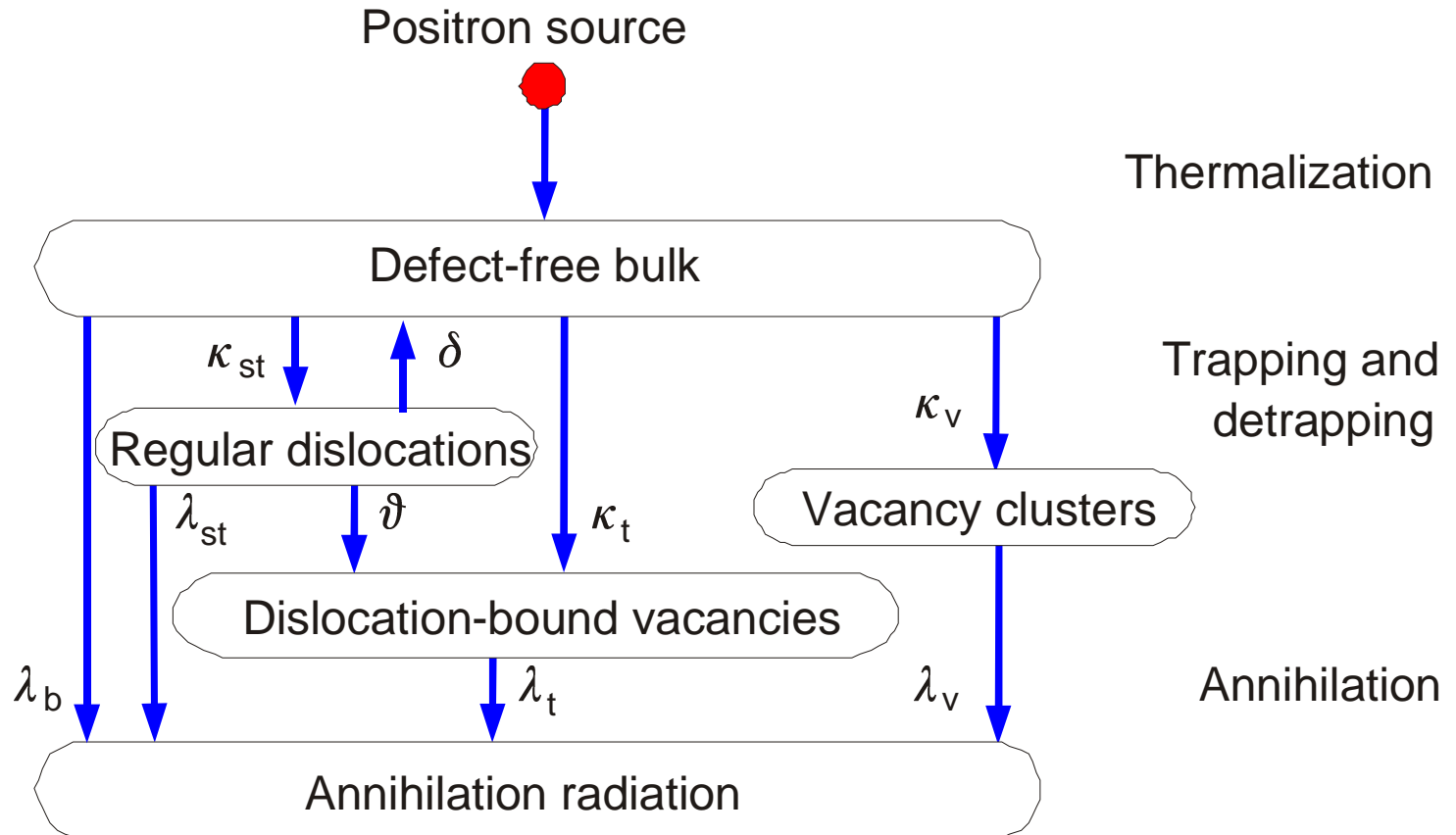


# Dislocations as positron traps



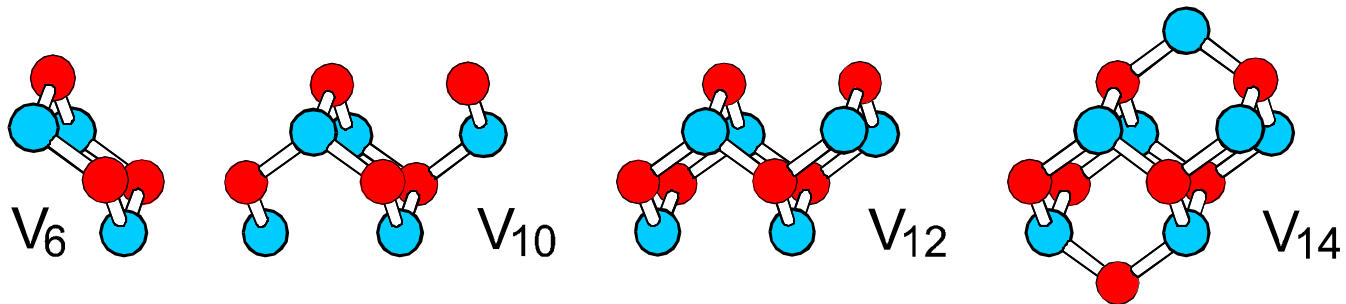
Positron potential  $V_+(x,y)$  of a dislocation. The regular dislocation line is a shallow positron trap, while a bound vacancy acts as a deep trap.

# Trapping model in deformed crystals



# Calculation of vacancy clusters

- Construction of vacancy clusters and relaxation with a self-consistent charge-density-functional-based tight binding (SCC DFTB) method [Eltner *et al.* 1998]
- Method allows the modeling of large supercells (512 atoms), which are needed to avoid defect–defect interactions.
- Different vacancy aggregates were examined in respect of their stability.
- Construction scheme of closed structures with hexagonal rings of vacancies gives clusters of lowest total energy

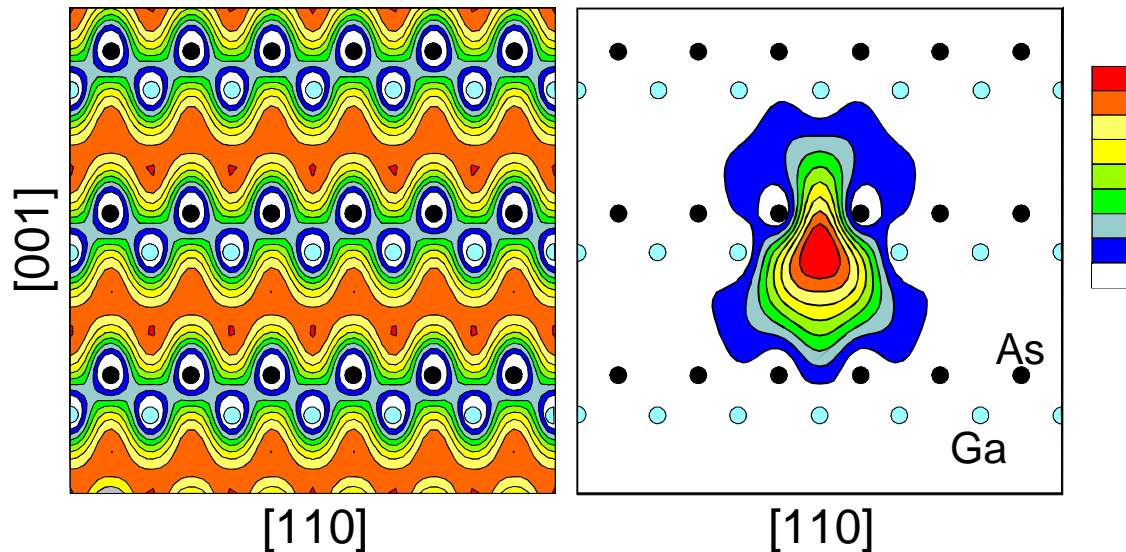


Structure of some unrelaxed  $V_n$  clusters in GaAs

# Calculation of the positron lifetime

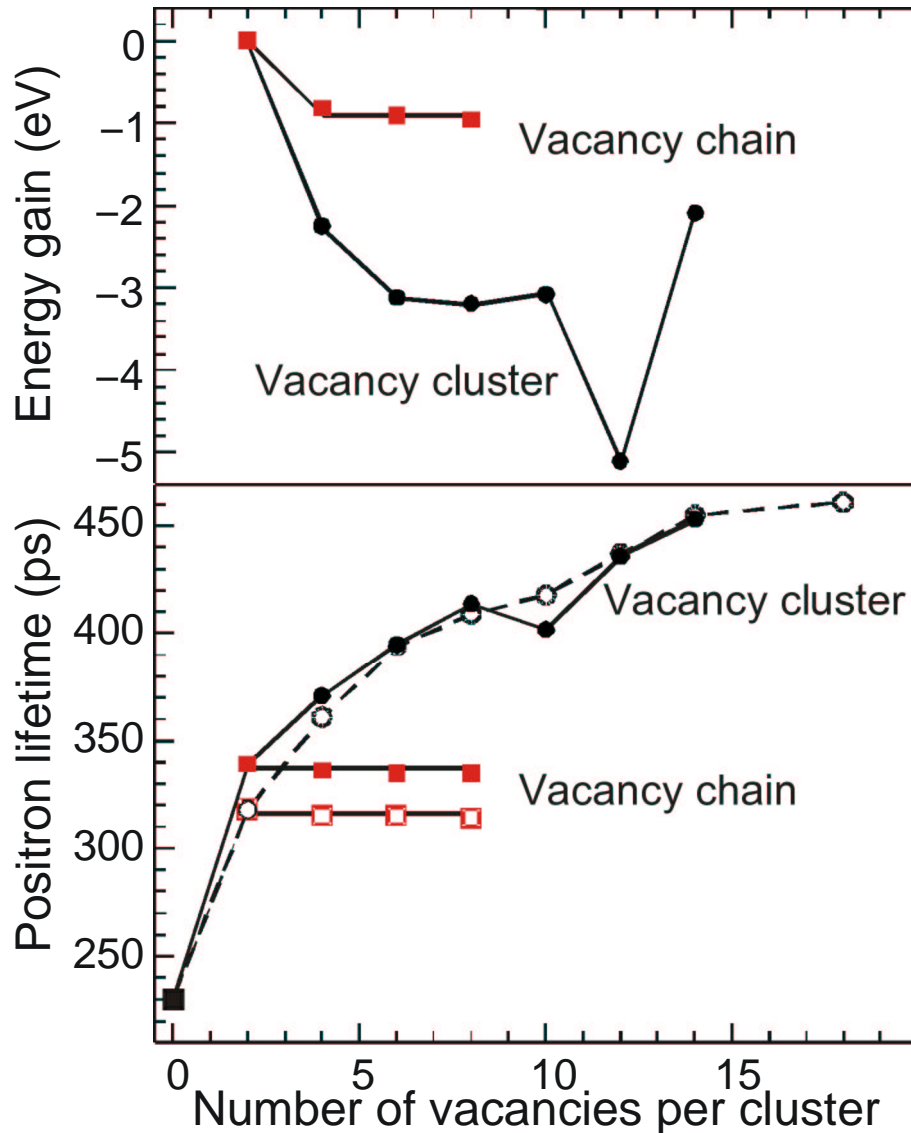
Calculation of positron lifetimes for various vacancy cluster configurations using the superimposed-atom model of Puska *et al.* (1989)

$$\text{Annihilation rate} \quad \lambda \propto \int \Gamma n^- |\Psi^+(\mathbf{r})|^2 d\mathbf{r}$$



Positron wave function in bulk GaAs (*left*) and in a gallium vacancy (*right*)

# Stability of vacancy clusters and cluster-related positron lifetimes

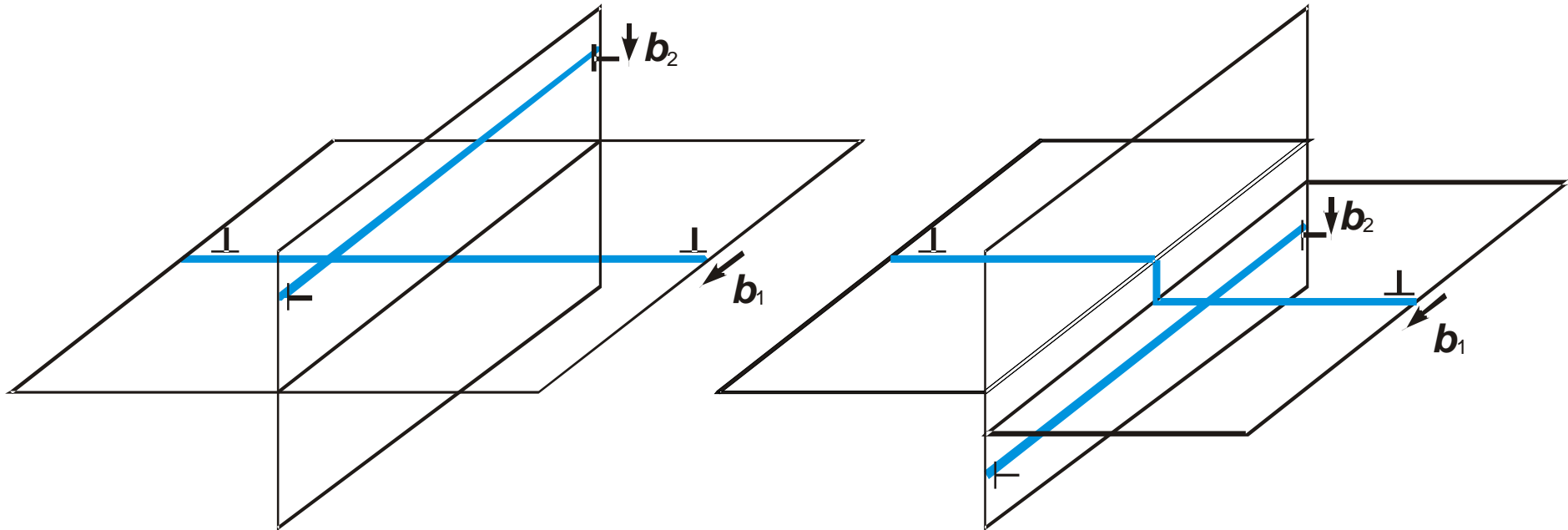


Energy gained by adding a divacancy to an aggregate of  $n - 2$  vacancies in GaAs (*upper part*) and positron lifetimes in vacancy aggregates (*lower part*). *Open/closed symbols:* configuration before/after relaxation.

# Results of calculations

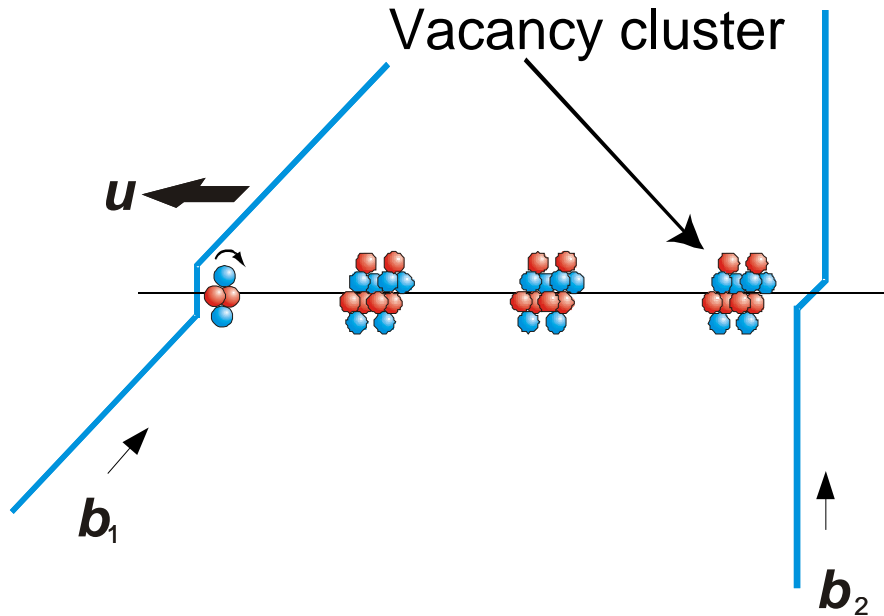
- Especially stable structures ( $n < 18$ ):  
 $V_{12}$  in GaAs  
 $V_6, V_{10}, V_{14}$  in Si
- Vacancy chains are not energetically favored structures
- The experimentally observed long-lived positron lifetime component may be attributed to  $V_{12}$  in GaAs and to  $V_{14}$  in Si.
- Magic numbers in silicon  $n = 4i + 2, i = 1, 2, 3, \dots$

# Cutting of dislocations



Cutting of edge dislocations

# Formation of vacancy clusters



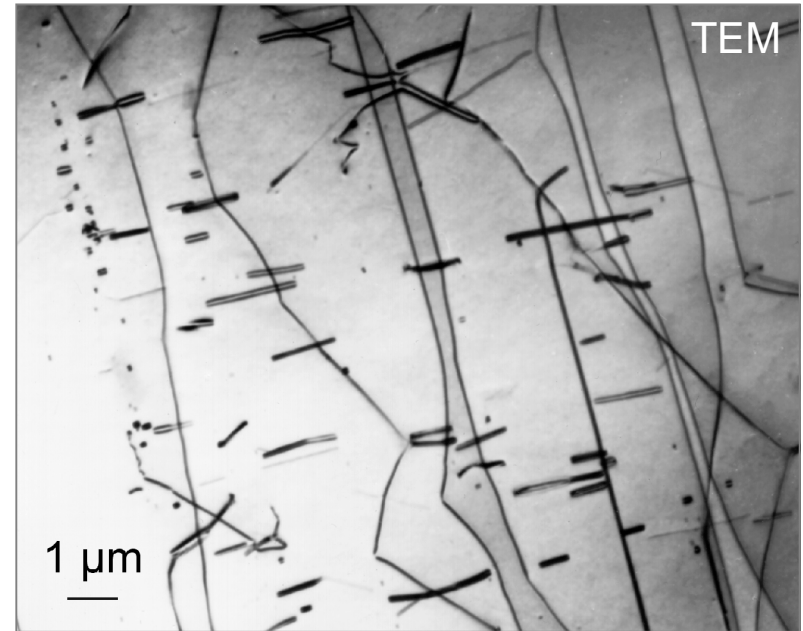
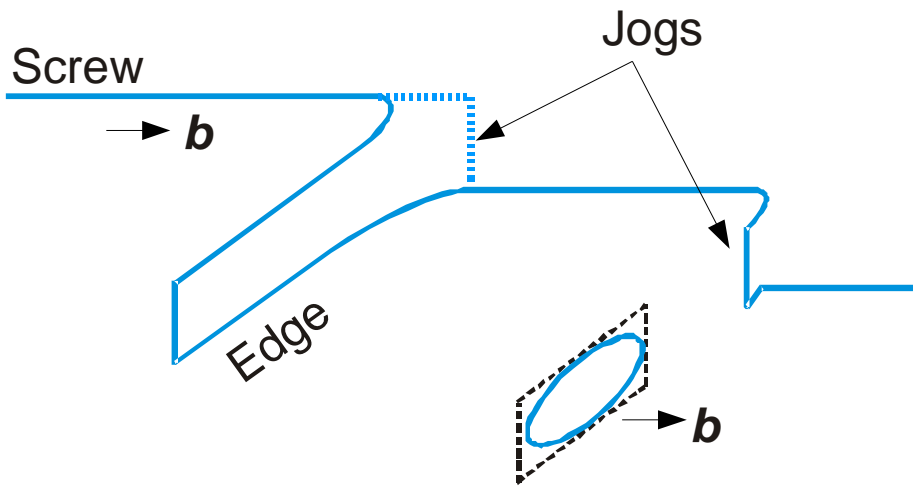
*Number of point defects*

$$C = \frac{1}{V} \frac{\xi_1 \cdot u \times \xi_2}{|\xi_1 \cdot u \times \xi_2|} b_1 \cdot u \times b_2$$

Agglomeration of vacancies as a result of jog dragging at screw dislocations

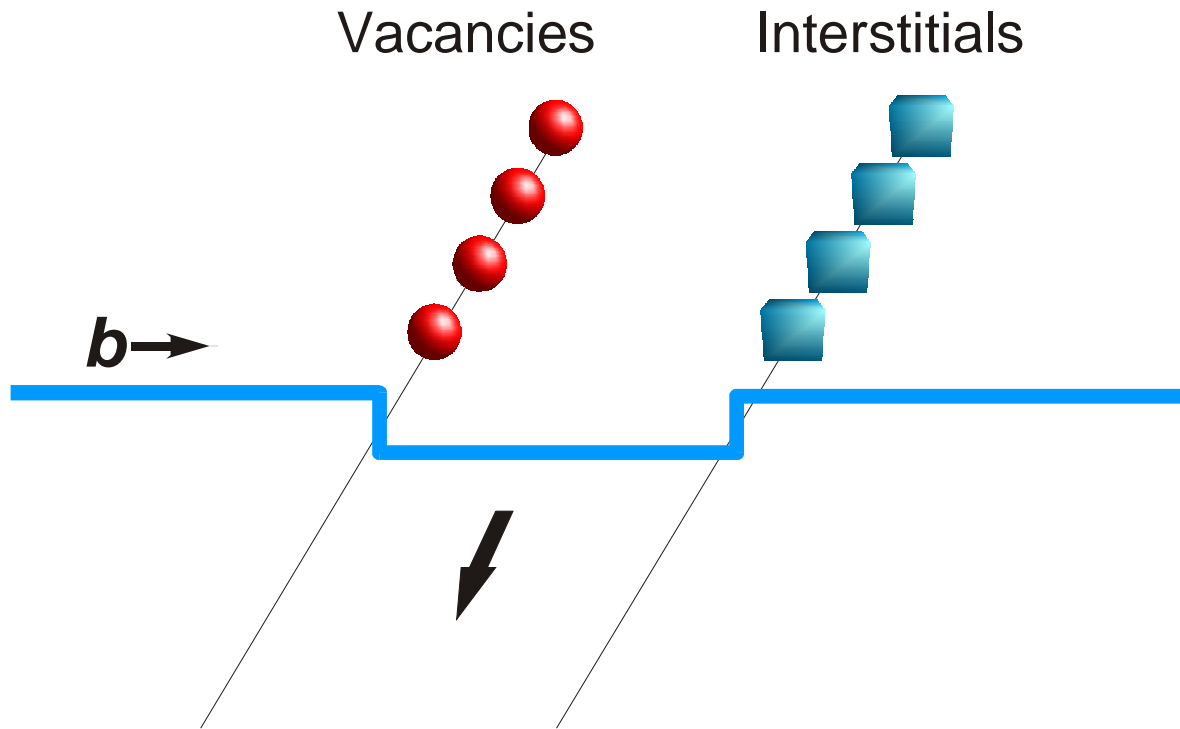


# Superjogs

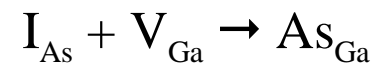
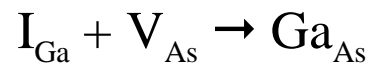


Formation of edge dipoles and prismatic dislocation loops

# Vacancies *and* interstitials



Secondary reactions lead to antisites:



# Summary

- ☑ The formation of point defects during plastic deformation of semiconductors can be related to dislocation motion.
- ☑ The basic mechanism is the emission of vacancies and interstitials by screw dislocations containing jogs.
- ☑ Formation of long rows of vacancies is energetically unfavorable.
- ☑ Stable three-dimensional vacancy agglomerates are formed in a primary process by atomic re-arrangement directly at the climbing jog.
- ☑ Dislocations are combined positron traps with the regular dislocation line representing a shallow positron trap and bound vacancies as deep traps.